Prediction of Kinematic Viscosities for Binary and Ternary Liquid Mixtures with an ASOG-VISCO Group Contribution Method¹

K. Tochigi,2*,*³ **K. Yoshino,**² **and V. K. Rattan**⁴

The kinematic viscosities for 273 binary and 11 ternary systems were predicted with a new model (ASOG-VISCO) developed by combining the ASOG group contribution method and Eyring's theory of absolute reaction rates. The ASOG-VISCO group pair parameters were determined from literature kinematic viscosity data for group pairs of $CH₂$, ArCH, CyCH, OH, H₂O, CO, COO, CCl₃, and CCl₄ in the temperature range of 283.15 to 333.15 K. The overall average deviations between experimental and predicted kinematic viscosities for the binary and ternary systems were 4.15 and 5.03%, respectively. The predicted results using ASOG-VISCO were better than those determined with the UNIFAC-VISCO group contribution method.

KEY WORDS: ASOG; group contribution method; kinematic viscosity; prediction.

1. INTRODUCTION

The kinematic viscosity of a liquid system is an important physicochemical property required for fluid transport calculations in chemical processes. Although the correlation and prediction of viscosity has been carried out by many researchers [1], the database for liquid mixtures is relatively small

¹Paper presented at the Sixteenth European Conference on Thermophysical Properties, September 1–4, 2002, London, United Kingdom.

²Department of Materials and Applied Chemistry, Nihon University, 1-8 Kanda-Surugadai, Chiyoda, Tokyo 101-8308, Japan.

³To whom correspondence should be addressed. E-mail: tochigi@chem.cst.nihon-u.ac.jp

⁴Department of Chemical Engineering and Technology, Panjab University, Chandigarh 160-014, India.

and so it is of interest to develop predictive methods. The absolute reaction rate theory of Eyring et al. [2] applicable to liquids could possibly be effective from a practical point of view, because it makes use of the excess Gibbs free energy [3–6], which can be combined with solution theory.

This paper proposes a group contribution method called ASOG-VISCO that combines the Eyring's model with the ASOG group contribution model [7]. By using ASOG-VISCO, the mixture kinematic viscosity can be evaluated from the known viscosity data of pure components and group pair parameters. Predictions were performed for 273 binary and 11 ternary data sets. The predicted results are compared with those by UNIFAC-VISCO [4].

2. EQUATIONS FOR CALCULATING KINEMATIC VISCOSITY

From Eyring's theory of absolute reaction rate [2–4], the kinematic viscosity *ν* is given as

$$
v = \frac{hN_{\rm A}}{M} \exp\left(\frac{\Delta^* \mathcal{G}}{RT}\right) \tag{1}
$$

where $\Delta^* G$ is the activation free energy in the flowing state, R is the universal gas constant, T is the absolute temperature, h is Plank's constant, *N*^A is Avogadro's number, and *M* is the molar mass. *∆*∗*G* is obtained from the ideal free energy of solution, *∆*∗*G*id, and the excess free energy *∆*∗*G*^E at the activation state as follows;

$$
\Delta^* G = \Delta^* G^{id} + \Delta^* G^E \tag{2}
$$

From Eqs. (1) and (2), the kinematic viscosity of a liquid mixture can be determined from the pure component values and the excess free energies of the activation,

$$
\ln(\nu M) = \sum_{i} x_i \ln(\nu_i M_i) + \frac{\Delta^* G^E}{RT}
$$
 (3)

where x_i is mole fraction of component *i*.

In order to calculte kinematic viscosity, we make use of the following equation similar to the relation [8] that is derived when the Eyring empirical constant [2] is set to 1.0;

$$
\ln(vM) = \sum_{i} x_i \ln(v_iM_i) - \frac{\Delta G^{E}}{RT}
$$
 (4)

Here ΔG^E is the excess Gibbs free energy at the equilibrium state.

3. DETERMINATION OF ASOG-VISCO GROUP PAIR PARAMETERS

In this work, *∆G*^E was evaluated from the ASOG group contribution method, that is, a predictive method for the activity coefficient γ_i , given by the following equations [7]:

$$
\frac{\Delta G^{E}}{RT} = \sum_{i} x_i \ln \gamma_i = \sum_{i} x_i \left(\ln \gamma_i^{FH} + \ln \gamma_i^{G} \right)
$$
 (5)

$$
\ln \gamma_i^{\text{FH}} = \ln \frac{v_i^{\text{FH}}}{\sum_{j} v_j^{\text{FH}} x_j} + 1 - \frac{v_i^{\text{FH}}}{\sum_{j} v_j^{\text{FH}} x_j}
$$
(6)

$$
\ln \gamma_i^G = \sum_k \nu_{k,i} \left(\ln \Gamma_k - \ln \Gamma_k^{(i)} \right) \tag{7}
$$

$$
\ln \Gamma_k = -\ln \sum_{l} X_l a_{k,l} + 1 - \sum_{l} \frac{X_l a_{l,k}}{\sum_{m} X_m a_{l,m}}
$$
(8)

$$
X_{l} = \frac{\sum_{i} x_{i} v_{l,i}}{\sum_{i} x_{i} \sum_{k} v_{k,i}}
$$
(9)

$$
a_{k,l} = \exp\left(m_{k,l} + \frac{n_{k,l}}{T}\right) \tag{10}
$$

Here, v_i^{FH} and $v_{k,i}$ are the number of atoms (other than hydrogen atoms) in molecule *i*, and in group *k* of molecule *i*, respectively. The Γ_k and $\Gamma_k^{(i)}$ are group activity coefficients of group *k* in the mixture and standard state (pure component *i*), and $m_{k,l}$ and $n_{k,l}$ in Eq. (10) are ASOG-VISCO group pair parameters.

The systems discussed in this study contain n-paraffins, alcohols, water, ketones, esters, chloroform, and carbon tetrachloride. These systems are composed of CH₂, ArCH, CyCH, OH, H₂O, CO, COO, CCl₃ and CCl4 groups.

The group pair parameters were determined from experimental kinematic viscosity data using the following objective function:

$$
F_{\text{obj.}} = \sum_{n=1}^{ND} \left| \frac{\nu_{\text{cal.}} - \nu_{\text{exp.}}}{\nu_{\text{exp.}}} \right|_n \tag{11}
$$

Table I shows the group pair parameters. The temperature range is 283.15−333.15 K.

$\lceil m \rceil$ l k					$CH2$ ArCH CyCH OH $H2O$	$\rm CO$	\rm{COO}	CCl ₃	CCl ₄
(a) $m_{k,l}$ CH ₂ ArCH CyCH OН H ₂ O $\rm CO$ COO CCl ₃ CCl ₄	θ 1.2817 Ω 14.146 0.0879 θ 0.0952 $\mathbf{0}$ $\overline{0}$	0.2779 Ω -1.543 0 $\overline{}$ 3.7286 -0.902 Ω 0.3971	θ -1.565 Ω -4.676 13.184 θ $-$ -2.335 1.3971	θ 1.0616 $\overline{0}$ 0.204 -11.32 19.131 2.3089	$-0.357 -9.006$ 0 $-$ -13.11 $\overline{0}$ -0.968 $\overline{}$ $\overline{}$ $\overline{}$	-1.109 3.4974 5.9432 0.2318 θ $\mathbf{0}$ 0.7525	0.3682 0.2418 θ -40.2 $\overline{}$ θ θ θ -4.048	θ θ 82.302 $\overline{}$ θ θ $\overline{}$	Ω 0.1759 0.9018 -3.874 -0.451 11.005 $\overline{}$ Ω
[n]									
(b) n_k, l CH ₂ ArCH CyCH OH H ₂ O CO \rm{COO} CCl ₃ CCl ₄	θ -187.4 $\mathbf{1}$ -6137 528 -460.5 -383.6 84.034 128.78	-418.5 Ω 368.21 -1247 -1922 -107.2 -98.59 -69.59	0.1004 510 θ 456.72 -4657 36.378 \equiv 496.69	469.65 280.63 0.9436 θ 537.65 3240.5 -5747 -306.4 -16.11	2216.5 $\overline{}$ $\overline{}$ 2964.1 θ -0.968 $-$ \equiv $\frac{1}{2}$	265.39 678.02 -765.5 -2071 94.521 θ 99.719 31.126	112.59 140.35 -183.8 11583 -108.3 θ 231.03 1480.7	-111.8 91.432 $-$ -27537 $\overline{}$ -277.9 θ $\overline{}$	-177 -1.857 -130.2 70.876 -270.9 -3780 $\overline{}$ $\overline{0}$

Table I. ASOG-VISCO Group Pair Parameters (283*.*15−333*.*15 K)

4. PREDICTED RESULTS

4.1. Binary Systems

The kinematic viscosities for binary systems were evaluated for 273 data sets as summarized in Table II. The overall average deviation between experimental [9, 10] and predicted kinematic viscosities was 4.15%. Table II shows the predicted results using ASOG-VLE [7] and UNIFAC-VISCO [4] parameters. The predictions using ASOG-VISCO were better than those made with UNIFAC-VISCO. Figure 1 shows predicted results for acetone $+$ ethanol system at 298.15 K. Figure 1 shows the results using ASOG-VLE parameters and UNIFAC-VISCO parameters. Figure 2 shows the results for ethanol + water system at 293*.*15−333*.*15 K.

4.2. Ternary Systems

The kinematic viscosities for ternary systems have been predicted for 11 datasets composed of hydrocarbons, alcohols, ketones, and esters. The

				ASOG-VISCO ASOG-VLE UNIFAC-VISCO			
System							
(1)	(2)	No. of data sets	No. of data points		$\Delta \nu(\%)$		
Alkanes	Alcohols	11	109	3.36	12.28	2.82	
Alkanes	Esters	25	249	2.5	9.44	0.73	
Alkanes	Ketones	7	92	1.05	19.37	1.68	
Alkanes	Cycloalkanes	5	28	10.42	10.5	4.73	
Alkanes	Aromatics	24	254	4.15	7.7	9.63	
Alcohols	Ketones	18	154	4.04	10.66	6.8	
Alcohols	Esters	$\overline{4}$	36	3.53	8.47	4.34	
Alcohols	Cycloalkane	21	187	2.13	16.42	2.36	
Alcohols	Aromatics	3	24	7.67	36.42	7.2	
Alcohols	Water	24	227	4.52	45.53	unavailable	
Aromatics	Esters	10	62	2.79	2.83	1.21	
Aromatics	Ketones	17	170	4.39	15.93	5.71	
Aromatics	Cycloalkanes	7	49	2.67	4.32	3.03	
Cycloalkanes	Esters	$\overline{4}$	36	2.19	7.84	12.09	
Cycloalkanes	Ketones	3	26	3.95	46.83	5.61	
Esters	Ketones	4	36	2.77	7.27	3.23	
Ketones	Water	6	49	13.51	56.53	unavailable	
Chloroform	Aromatics	$\overline{2}$	16	3.07	\overline{a}	unavailable	
Chloroform	Alkanes	1	8	0.36	$\overline{}$	unavailable	
Chloroform	Esters	1	$\overline{7}$	2.21	$\overline{}$	unavailable	
Chloroform	Alcohols	14	91	6.98	$\overline{}$	unavailable	
CCl ₄	Aromatics	5	38	1.84	\equiv	unavailable	
CCl ₄	Ketones	$\overline{4}$	46	0.84	$\overline{}$	unavailable	
CCl ₄	Esters	9	64	1.34	$\overline{}$	unavailable	
CCl ₄	Cycloalkanes	3	21	1.54	$\overline{}$	unavailable	
CCl ₄	Alcohols	41	394	6.45	\equiv	unavailable	
Overall (including water)		273	2473	4.15	17.27		
Overall		243	2197	3.90	11.76	4.59	

Table II. Predicted Results of Kinematic Viscosity for Binary Liquid Mixtures using ASOG-VISCO, ASOG-VLE, and UNIFAC-VISCO(283.15−333.15 K)

overall average deviation between experimental [9] and predicted kinematic viscosity as shown in Table III is 5.03%.

5. CONCLUSIONS

A predictive model was developed based on the ASOG group contribution method and Eyring's absolute reaction rate theory. Calculations made with the model show that kinematic viscosities can be predicted

Fig. 1. Kinematic viscosity for acetone (1) + ethanol (2) system at 298.15 K.

Fig. 2. Kinematic viscosity for ethanol (1) + water (2) system at 293.15, 313.15, and 333.15 K.

to within 4.2% for binary mixtures and 5.0% for ternary mixtures for the literature data studied. The model requires only pure component kinematic viscosities and molecular structure.

	System		ASOG-VISCO $\Delta \nu(\%)$	
(1)	(2)			
Ethanol	Acetone	Cyclohexane	12	4.73
Acetone	Hexane	Ethanol	12	1.99
Acetone	Ethanol	Methanol	12	12.09
Acetone	Hexane	Cyclohexane	12	1.75
Hexane	Cyclohexane	Ethanol	12	4.29
Methanol	Ethanol	2-Propanol	12	2.83
Acetone	Ethanol	2-Propanol	12	8.63
Ethanol	Cyclohexane	2-Propanol	12	2.43
Methyl acetate	Cyclohexane	Ethanol	12	1.67
Methanol	Ethanol	1-Propanol	12	1.61
Toluene	1-Hexanol	Benzyl alcohol	24	7.51
Overall			136	5.03

Table III. Predicted Results of Kinematic Viscosity for Ternary Liquid Mixtures using ASOG-VISCO

ACKNOWLEDGMENTS

This work was partially supported by a Grant-in-Aid for Scientific Research (c) awarded by the Ministry of Education, Sports and Culture, Japan (Grant No. 14550744).

REFERENCES

- 1. B. P. Poling, J. M. Prausnitz and J. P. O'Connell, *The Properties of Gases and Liquids*, *5th Ed.* (McGraw-Hill, New York, 2001).
- 2. H. Eyring, R. E. Powell and W. E. Roseveare, *Ind. End. Chem*. **33**:430 (1941).
- 3. D. T. Wu, *Fluid Phase Equilib*. **30**:149 (1986).
- 4. J. L. Chevalier, P. Petrino and Y. Gaston-Bonhomme, *Chem. Eng. Sci*. **143**:1303 (1988).
- 5. W. Cao, Aa. Fredenslund and P. Rasmussen, *Ind. Eng. Chem. Res*. **31**:2603 (1992).
- 6. R. J. Martins, M. J. E. M. Cardoso and O. E. Barcia, *Ind. Eng. Chem. Res*. **39**:849 (2000).
- 7. K. Tochigi, D. Tiegs, J. Gmehling and K. Kojima, *J. Chem. Eng. Japan* **23**:453 (1990).
- 8. L. T. Novak, *Ind. Eng. Chem. Res*. **42**:1824 (2003).
- 9. The Society of Chemical Engineers, Japan, *Physico-Chemical Properties for Chemical Engineering*, Vols. 1 to 21 (Maruzen and Kagaku Kougyousha, Tokyo, 1977–2000).
- 10. K. Stephan and H. Heckenberger, *Thermal Conductivity and Viscosity Data of Fluid Mixtures*, DECHEMA Chemistry Data Series, Vol. X, Part 1 (DECHEMA, Frankfurt am Main, 1988).
- 11. I. C. Wei and R. L. Rowley, *Chem. Eng. Sci*. **40**:401 (1985).
- 12. K. Noda, Y. Aono and K. Ishida, *Kagaku Kogaku Ronbunshu* **9**:237 (1983).